2003 AMC 8

Time limit: 40 minutes

Typeset by: LIVE, by Po-Shen Loh

https://live.poshenloh.com/past-contests/amc8/2003

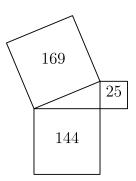


Copyright: Mathematical Association of America. Reproduced with permission.

- 1. Jamie counted the number of edges of a cube, Jimmy counted the numbers of corners, and Judy counted the number of faces. They then added the three numbers. What was the resulting sum?
 - A 12
 - в 16
 - c 20
 - D 22
 - E 26
- 2. Which of the following numbers has the smallest prime factor?
 - A 55
 - в 57
 - c 58
 - D 59
 - E 61

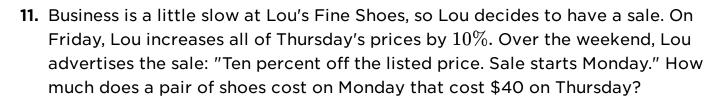
3.		rger at Ricky C's weighs 120 grams, of which 30 grams are filler. What ent of the burger is not filler?	
	A	60%	
	В	65%	
	С	70%	
	D	75%	
	E	90%	
4.	4. A group of children riding on bicycles and tricycles rode past Billy Bob's here 6 0. Billy Bob counted 7 0 children and 19 0 wheels. How many tricycles were there		
	A	2	
	В	4	
	С	5	
	D	6	
	E	7	
5. If 20% of a number is $12,$ what is 30% of the same number?		% of a number is $12,$ what is $30%$ of the same number?	
	A	15	
	В	18	
	С	20	
	D	24	
	E	30	

6. Given the areas of the three squares in the figure, what is the area of the interior triangle?



- A 13
- в 30
- c 60
- D 300
- E 1800
- 7. Blake and Jenny each took four 100-point tests. Blake averaged 78 on the four tests. Jenny scored 10 points higher than Blake on the first test, 10 points lower than him on the second test, and 20 points higher on both the third and fourth tests. What is the difference between Jenny's average and Blake's average on these four tests?
 - A 10
 - в 15
 - c 20
 - D 25
 - E 40

8.	Who gets the fewest cookies from one batch of cookie dough?		
	A	\mathbf{Art}	
	В	Roger	
	С	Paul	
	D	Trisha	
	E	There is a tie for fewest.	
	Art's cookies sell for $60 \rlap/c$ each. To earn the same amount from a single batch, how much should one of Roger's cookies cost?		
	A	18 c	
	В	25 m c	
	С	40 m c	
	D	75 m c	
	E	90 m c	
10.	How	many cookies will be in one batch of Trisha's cookies?	
		10	
	В	12	
	С	16	
	D	18	
	E	24	



A \$36 B \$39.60

c \$40

D \$40.40

E \$44

12. When a fair six-sided dice is tossed on a table top, the bottom face cannot be seen. What is the probability that the product of the faces that can be seen is divisible by 6?

A $\frac{1}{3}$

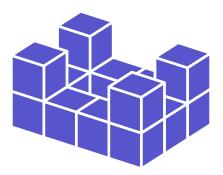
 $\mathsf{B} \qquad \frac{1}{2}$

C $\frac{2}{3}$

D $\frac{5}{6}$

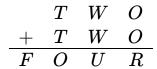
E 1

13. Fourteen white cubes are put together to form the figure on the right. The complete surface of the figure, including the bottom, is painted purple. The figure is then separated into individual cubes. How many of the individual cubes have exactly four purple faces?



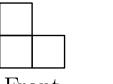
- A 4
- в 6
- c 8
- D 10
- E 12

14. In this addition problem, each letter stands for a different digit.



If T=7 and the letter ${\cal O}$ represents an even number, what is the only possible value for W?

- **A** 0
- в 1
- c 2
- D 3
- E 4
- **15.** A figure is constructed from unit cubes. Each cube shares at least one face with another cube. What is the minimum number of cubes needed to build a figure with the front and side views shown?



Front



- A 3
- в 4
- **c** 5
- D 6
- E 7

16.	. Ali, Bonnie, Carlo and Dianna are going to drive together to a nearby theme park.
	The car they are using has four seats: one driver's seat, one front passenger seat
	and two back passenger seat. Bonnie and Carlo are the only ones who know how
	to drive the car. How many possible seating arrangements are there?

A 2

в 4

c 6

D 12

E 24

17. The six children listed below are from two families of three siblings each. Each child has blue or brown eyes and black or blond hair. Children from the same family have at least one of these characteristics in common. Which two children are Jim's siblings?

Child	Eye Color	Hair Color
Benjamin	Blue	Black
Jim	Brown	Blond
Nadeen	Brown	Black
Austin	Blue	Blond
Tevyn	Blue	Black
Sue	Blue	Blond

A Nadeen and Austin

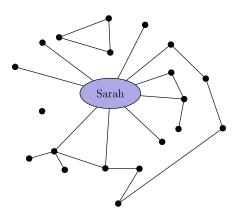
B Benjamin and Sue

c Benjamin and Austin

D Nadeen and Tevyn

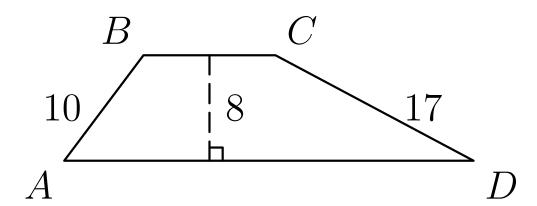
E Austin and Sue

18. Each of the twenty dots on the graph below represents one of Sarah's classmates. Classmates who are friends are connected with a line segment. For her birthday party, Sarah is inviting only the following: all of her friends and all of those classmates who are friends with at least one of her friends. How many classmates will not be invited to Sarah's party?



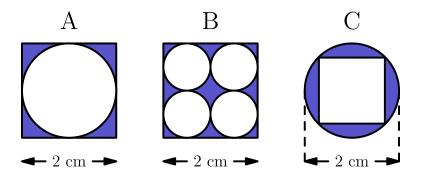
- A 1
- в 4
- c 5
- D 6
- E 7
- **19.** How many integers between 1000 and 2000 have all three of the numbers 15,20, and 25 as factors?
 - A 1
 - в 2
 - c 3
 - D 4
 - E 5

- **20.** What is the measure of the acute angle formed by the hands of the clock at $4:\ 20\ \text{a.m.}$?
 - A 0°
 - в 5°
 - c 8°
 - D 10°
 - E 12°
- **21.** The area of trapezoid ABCD is $164~\rm cm^2$. The altitude is $8~\rm cm$, AB is $10~\rm cm$, and CD is $17~\rm cm$. What is BC, in centimeters?



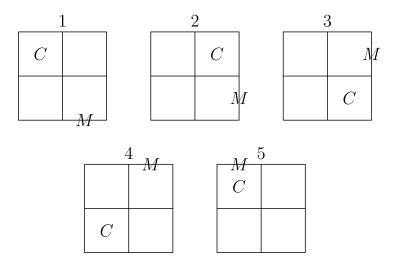
- A 9
- в 10
- c 12
- D 15
- E 20

22. The following figures are composed of squares and circles. Which figure has a shaded region with largest area?



- A A only
- B B only
- c C only
- E all are equal

23. In the pattern below, the cat moves clockwise through the four squares and the mouse moves counterclockwise through the eight exterior segments of the four squares.



If the pattern is continued, where would the cat and mouse be after the $247\mathrm{th}$ move?

Α

В

С

D

Ε



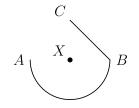


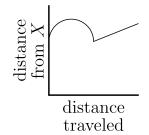


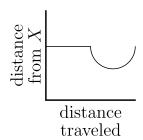


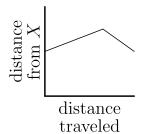
3.6	C	
		7 A

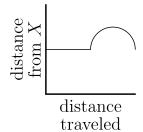
24. A ship travels from point A to point B along a semicircular path, centered at Island X. Then it travels along a straight path from B to C. Which of these graphs best shows the ship's distance from Island X as it moves along its course?

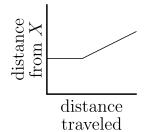












Α

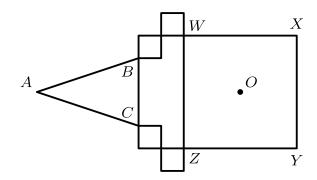
В

С

D

Ε

25. In the figure, the area of square WXYZ is $25~\mathrm{cm}^2$. The four smaller squares have sides $1~\mathrm{cm}$ long, either parallel to or coinciding with the sides of the large square. In $\triangle ABC$, AB = AC, and when $\triangle ABC$ is folded over side \overline{BC} , point A coincides with O, the center of square WXYZ. What is the area of $\triangle ABC$, in square centimeters?



- $\begin{array}{|c|c|} \hline & & 15 \\ \hline & 4 \\ \hline \end{array}$
- $\begin{array}{c|c} B & \frac{21}{4} \end{array}$
- $c \frac{27}{4}$
- D $\frac{21}{2}$
- $\frac{27}{2}$

Solutions: https://live.poshenloh.com/past-contests/amc8/2003/solutions

